

# **Design of Passivity Based Robust Control of AC / DC Power Converter for Power Factor Improvement and Voltage Regulation**

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## *Abstract:*

In this work an Interconnection-and-Damping Assignment Passivity-based control (IDA-PBC) for a full-bridge rectifier is investigated. The controller design takes advantage of the generalized state space averaging (GSSA) modeling technique to convert the quoted nonstandard problem (in actual variables) into a standard regulation one (in GSSA variables). The transient behavior of the system, along with the controller is obtained through computer simulation. The closed-loop system performance fulfils unity power factor in the AC mains and output DC voltage regulation. In particular, the technique is shown to be effective and robust with respect to load variations.

*Key terms:* Passivity Based Control, Generalized State Space Averaging (GSSA), AC-DC power converter.

## **1. INTRODUCTION**

In recent years, single-phase switch-mode AC/DC power converters have been increasingly used in the industrial, commercial, residential, aerospace, and military environment. To get constant output voltage and near unity power factor, it is essential that the converter has to be controlled [1]. In recent power electronic researches, high power density, high power factor, high efficiency, low current distortion, and simple control scheme are strongly recommended for the industrial applications [2]. This is due to the enforcement of strict harmonic regulations such as IEC 1000-3-2. Voltage source converters provide excellent control over power flow in both directions. They can be operated as AC–DC converters to generate regulated DC voltage at high input

power factor. The power flow can easily be reversed to operate the converter as a DC–AC converter [3]. This capability makes the system ideally suited to electric drives and line interactive UPS applications. Conventional diode rectifiers or phase-controlled rectifiers have properties of simple structure and low cost. However, they have the inherent drawbacks that the power factor decreases when the firing angle increases and the line current harmonics are relatively high. To overcome the above problems, several circuit topologies of the single-phase switching mode rectifier (SMR) with low current distortion and unity power factor have been proposed in the past few years [4]. These circuit configurations are based on the full bridge diode rectifier followed by a boost, buck boost, or cuk converter. Single-phase full bridge and half bridge SMR circuit configurations have capabilities of bidirectional power flow, reactive power control, and high power factor.

Among these circuit topologies, single-phase unidirectional AC/DC converters with boost topology have been widely used as front-end power factor pre-regulator due to its good performance characteristics. The boost topology has properties of high power factor, low current distortion, step-up voltage ratio and continuous input current. Boost rectifier topologies can be broadly classified as continuous mode and discontinuous mode conduction rectifiers [5]. The single-phase two-level PWM continuous current mode rectifier with unidirectional power flow is presented here.

The generalized state-space averaging method is a way to model the power converters as time independent systems, defined by unified set of differential equations, capable of representing circuit waveforms without discontinuities [6]. Consequently, this approach is not suitable for modeling converters which have dominant oscillatory behavior such as the resonant type converters or large ripple PWM converters [7]. Therefore, analysis of AC/DC power converters with ideal switches and parasitic components (capacitors or inductors) forming loops must be considered with more care. With the generalized state-space averaging method, the circuit state variables are approximated by a Fourier series expansion with time-dependent coefficients [8]. This representation results in an unified time-invariant set of differential

equations where the state variables are the coefficients of the corresponding Fourier series of the circuit variables.

The paper is organized as follows. Section 2 studies the dynamics of a single-phase full-bridge boost converter circuit and develops a state space model. In section 3, the converter model is analyzed in the frame of Port-Controlled Hamiltonian System (PCHS) form. Section 4 presents the controller design based on IDA-PB control technique. The simulation results are shown in section 5 for the robustness and effectiveness of the technique employed. Finally some concluding remarks are drawn.

## 2. PROPOSED BOOST RECTIFIER

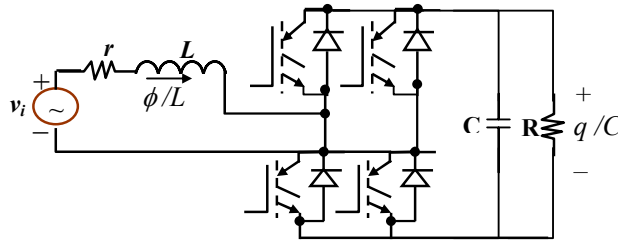


Figure 1 Single phase Full-bridge Boost Rectifier

Figure 1 shows the single phase full-bridge boost rectifier. The transistor works as a switch, which is turned on and off by the PWM control signal.

### 2.1 State Space Modeling:

The system behaviour is obtained by solving the modelling equations. Mathematical modelling also decides the details of the system that can possibly be studied by computer simulation. The starting point for modelling a converter, however, is by application of Kirchoff's and Ohm's law to the circuit, which provides first-order differential equations describing the state of current through inductor(s) and voltage across capacitor(s).

The following equations describe the dynamical behaviour of the full-bridge boost type rectifier in Figure 1.

$$\begin{aligned}\frac{d\phi(t)}{dt} &= \frac{-u(t)}{C}q(t) - \frac{r}{L}\phi(t) + V_i(t) \\ \frac{dq(t)}{dt} &= \frac{u(t)}{L}\phi(t) - i_l(t)\end{aligned}\quad (2.1)$$

where  $\phi(t)$  is the magnetic flux through inductor,  $q(t)$  is the electrical charge in capacitor,  $r$  is a resistance modelling the parasitic resistive effect of the inductor and the switches,  $u(t)$  describes the position of the switches taking values in the discrete set,  $i_l(t)$  is the load current, and  $V_i(t) = E \sin(\omega_0 t)$  is the AC voltage source of amplitude and angular frequency  $\omega_0 = 2\pi f$ ,  $f$  being the frequency in Hertz.

In this section, and for GSSA modelling purposes, the load will be assumed resistive, then  $i_l(t) = q(t)/RC$ .

A useful variable transformation, which simplifies (2.1), forthcoming developments, is obtained through  $v(t) = -u(t)q(t)$  and  $z = [z_1 \ z_2] = [\phi(t), (1/2)q(t)^2]$ . The system in the new variables is,

$$\frac{dz_1(t)}{dt} = \frac{-rz_1(t)}{L} + \frac{v(t)}{C} + v_i(t) \quad (2.2)$$

$$\frac{dz_2(t)}{dt} = \frac{-v(t)z_1(t)}{L} - i_l(t)\sqrt{2z_2(t)} \quad (2.3)$$

The energy in the storing elements and of this system can be described by,

$$H_T(t) = \frac{z_1(t)^2}{2L} + \frac{z_2(t)}{C} \quad (2.4)$$

And (2.2) & (2.3) can be rewritten as

$$\begin{bmatrix} \frac{dz_1(t)}{dt} \\ \frac{dz_2(t)}{dt} \end{bmatrix} = \begin{bmatrix} 0 & v \\ -v & 0 \end{bmatrix} \frac{\partial H_T}{\partial z} - \begin{bmatrix} r & 0 \\ 0 & C i_l \sqrt{2z_2} \end{bmatrix} \frac{\partial H_T}{\partial z} + \begin{bmatrix} v_i \\ 0 \end{bmatrix} \quad (2.5)$$

This corresponds to a PCHS system of the form,

$$\dot{z} = [J_T(v) - R_T(x)] \frac{\partial H_T}{\partial z}(z) + g_T \quad (2.6)$$

Where  $J_T = -J_T^T$ ,  $R(x) = R^T(x) \geq 0$  are the matrices describing the interconnection structure and damping, respectively. The last inequality results from and because

the load voltage is non negative. The input voltage is considered as an external disturbance modelled by vector. In order to obtain the simplest coherent GSSA model, let us determine the harmonic content of the states and the input in steady state.

### 2.3 Steady State Analysis

To this end, let  $z_1^*(t) = LI_d \sin(\omega_0 t)$  be the desired dynamics and  $i_l(t)$  be the load current assuming a resistive load. In order to obtain the steady-state zero dynamics, let us take into account this assumption in (2.5) – (2.6) and let us solve for  $v$  and  $z_2$ . The steady-state response yields,

$$z_2^*(t) = \alpha_{z_2} + \beta_{z_2} \sin(2\omega_0 t + \theta_{z_2}) \quad (2.7)$$

$$v^*(t) = C(E - rI_d) \sin(\omega_0 t) + I_d \omega_0 LC \cos(\omega_0 t) \quad (2.8)$$

Where,

$$\alpha_{z_2} = \frac{I_d RC^2}{4} (E - rI_d);$$

$$\beta_{z_2} = \frac{I_d RC^2}{4} \sqrt{\frac{(E - rI_d)^2 + (I_d \omega_0 L)^2}{1 + (\omega_0 RC)^2}}$$

$$\tan(\theta_{z_2}) = \frac{(E - rI_d) - \omega_0 RC(I_d \omega_0 L)}{\omega_0 RC((E - rI_d) + (I_d \omega_0 L))}$$

The value of parameter  $I_d$  can be obtained through power balance.

$$I_d = \frac{E}{2r} \mp \sqrt{\left(\frac{E}{2r}\right)^2 - \frac{2V_d^2}{rR}} \quad (2.9)$$

The minus sign has been chosen since it yields a stable equilibrium point with lower power consumption. The total stored energy in steady-state results in,

$$H_T(t) = \alpha_H + \beta_H \sin(2\omega_0 t + \theta_H) \quad (2.10)$$

Where,

$$\alpha_H = \frac{I_d CR}{4}(E - rI_d) + \frac{LI_d^2}{4}$$

$$\beta_H = \frac{\alpha_H = \frac{I_d CR}{4}(E - rI_d) + \frac{LI_d^2}{4}}{\sqrt{1 + (\omega_o RC)^2}}$$

$$\tan(\theta_H) = \frac{1}{\omega_o RC}$$

Expressions (2.1), (2.7), and (2.8) show that a suitable GSSA model of the system, useful for controller design purposes, should contemplate the first harmonic Fourier components for  $z_1(t)$ , the zero and second harmonic Fourier components for  $z_2(t)$  and the first harmonic Fourier components for  $v(t)$ . As for the Hamiltonian  $H_T(t)$ , from (2.10), the DC component and second harmonic should be considered. If, in addition, C is chosen to obtain a low voltage ripple in the capacitor, then  $\beta_{z2}$  and  $\beta_H$  are negligible with respect to  $\alpha_{z2}$  and  $\alpha_H$ , respectively. Hence, the second harmonic Fourier components of  $z_2(t)$  and  $H_T(t)$  will not be considered from now on.

### 3. FULL BRIDGE RECTIFIER AS A PCH SYSTEM IN GSSA VARIABLES

Although the most general GSSA model of a system has infinite dimension, the harmonic contents of signals in steady state can be used to find accurately enough finite dimensional GSSA models. To this aim, using (2.3) and taking into account the Fourier components we have considered as relevant, the bilinear product  $v(t)z_1(t)$  in (2.3) can be approximated as,

$$\langle vz_1 \rangle_0 = \sum_{k=-\infty}^{\infty} \langle v \rangle_{-k} \langle z_1 \rangle_k \approx 2(\langle v \rangle_1^R \langle z \rangle_1^R + \langle v \rangle_1^I \langle z_1 \rangle_1^I) \quad (3.1)$$

Furthermore,

$$\langle i_1 q \rangle_0 \approx 2(\langle i_l \rangle_1^R \langle q \rangle_1^R + \langle q \rangle_1^I \langle i_1 \rangle_1^I) + \langle i_l \rangle_0 \langle q \rangle_0 \quad (3.2)$$

As it has been assumed  $q(t)$  has predominantly DC harmonic components, the complex coefficients of order one in (3.1) will be discarded. Hence, using (3.1) and (3.2), the GSSA model of the system defined by (2.3) becomes,

$$\begin{aligned}\frac{d\langle z_2 \rangle_0}{dt} &= -\langle i_l \rangle_0 \sqrt{2\langle z_2 \rangle_0} - \frac{2}{L} \langle v \rangle_1^R \langle z_1 \rangle_1^R - \frac{2}{L} \langle v \rangle_1^I \langle z_1 \rangle_1^I \\ \frac{d\langle z_1 \rangle_1^R}{dt} &= -\frac{r}{L} \langle z_1 \rangle_1^R + \frac{1}{C} \langle v \rangle_1^R + \omega_0 \langle z_1 \rangle_1^I \\ \frac{d\langle z_1 \rangle_1^I}{dt} &= -\frac{r}{L} \langle z_1 \rangle_1^I + \frac{1}{C} \langle v \rangle_1^I + \omega_0 \langle z_1 \rangle_1^R - \frac{E}{2}.\end{aligned}\quad (3.3)$$

Let,  $x = [\langle z_2 \rangle_0, \langle z_1 \rangle_1^R, \langle z_1 \rangle_1^I]$  be the state and  $u = [\langle v_1 \rangle_1^R, \langle v_1 \rangle_1^I]$  control vectors, respectively, and

$$x^* = \left[ \frac{C^2 V_d^2}{2}, 0, \frac{-LI_d}{2} \right] \quad (3.4)$$

be the desired equilibrium.

The original control problem has become a regulation problem in the GSSA domain. For simplicity, let us denote the load current DC component by  $I_0 = \langle i_l \rangle_0$ . Then, the system in (3.3) can be written as the PCH system:

$$\begin{bmatrix} \frac{dx_1(t)}{dt} \\ \frac{dx_2(t)}{dt} \\ \frac{dx_3(t)}{dt} \end{bmatrix} = \begin{bmatrix} 0 & -u_1 & -u_2 \\ u_1 & 0 & \frac{\omega_0 L}{2} \\ u_2 & -\frac{\omega_0 L}{2} & 0 \end{bmatrix} \frac{\partial H}{\partial x} - \begin{bmatrix} CI_0 \sqrt{2x_1} & 0 & 0 \\ 0 & \frac{r}{2} & 0 \\ 0 & 0 & \frac{r}{2} \end{bmatrix} \frac{\partial H}{\partial x} + \begin{bmatrix} 0 \\ 0 \\ -\frac{E}{2} \end{bmatrix} \quad (3.5)$$

Or in a more compact form,

$$\dot{x} = [J(u) - R(x)] \frac{\partial H}{\partial x} + g \quad (3.6)$$

where,  $J(u)$  and  $R(x)$  are the interconnection-and-damping matrices, respectively, and  $g$  vector models an external disturbance. Note that  $H(x)$  is the DC component of the Hamiltonian in  $H_T(z)$  in (2.10); i.e.,

$$H(x) = \frac{1}{C} \langle z_2 \rangle_0 + \frac{1}{L} \langle \phi \rangle_1^{R^2} + \frac{1}{L} \langle \phi \rangle_1^{I^2} \quad (3.7)$$

$$\text{or, } H(x) = \frac{1}{C} x_1 + \frac{1}{L} x_2^2 + \frac{1}{L} x_3^2 \quad (3.8)$$

The GSSA system in (3.6) preserves the PCH structure of the system in (3.6), with the remarkable advantage of a regulation control objective. This allows the IDA passivity based design approach to be methodically used. In this line, an IDA-PB control fulfilling system specifications is designed in the next section. The control law depends on the output voltage DC component and requires measuring the dc output current to guarantee robustness with respect to load variations.

#### 4. CONTROLLER DESIGN

The final objective of the IDA-PBC approach [8] is to design a feedback control  $u = \beta(x)$ , such that the closed-loop dynamics is the PCH reference system.

$$\dot{x} = [J_d(x) - R_d(x)] \frac{\partial H_d}{\partial x}(x)$$

where,  $J_d(x) = -J_d^T(x)$  and  $J_d(x) = R_d^T(x) \geq 0$  are targeted interconnection-and-damping matrices, and the new energy function  $H_d(x) = H(x) + H_a(x)$  has a strict local minimum at the desired equilibrium.

##### 4.1 Conditions for Stable Equilibrium:

Following [8], we proceed in the standard manner.

(i) *Structure preservation.*

Given  $J_d(x)$  and  $R_d(x)$ , let  $J_a(x)$  and  $R_a(x)$  be defined by,

$$J_d(x) = J(x, \beta(x)) + J_a(x) = [J(x, \beta(x)) + J_a(x)]^T$$

$$R_d(x) = R(x) + R_a(x) = [R(x) + R_a(x)]^T$$

Then, the desired dynamics is achieved if it is possible to find functions  $\beta(x)$  and  $k(x) := \partial H_a(x) / \partial x$  satisfying,

$$[J(x, \beta(x)) + J_a(x) - (R(x) + R_a(x))] k(x) = - [J_a(x) - R_a(x)] \partial H_a(x) / \partial x + g.$$

(ii) *Integrability.*

$K(x)$  is the gradient of a scalar function.

That is,  $\frac{\partial k_i}{\partial x_j}(x) = \frac{\partial k_j}{\partial x_i}(x)$ .

(iii) *Equilibrium condition.*

$$\frac{\partial H_d}{\partial x}(x^*) = 0$$

If conditions (i) – (iii) hold, then  $x^*$  is a (locally) stable equilibrium point of the closed-loop system.

Let us particularise the aforementioned procedure for the full bridge boost rectifier controller defining  $J_d(x) = J(x, \beta(x))$  and  $R_d(x) = R(x)$ ,

i.e.,  $J_a(x) = 0$  and  $R_a(x) = 0$

## 4.2 Structure Preservation

Equation (1) yields,

$$0 = -I_0 C \sqrt{2 x_1 k_1} - u_1 k_2 - u_2 k_3 \quad (4.1)$$

$$0 = u_1 k_1 - \frac{r}{2} + \frac{\omega L}{2} k_3 \quad (4.2)$$

$$0 = u_2 k_1 - \frac{\omega L}{2} k_2 + \frac{E}{2} \quad (4.3)$$

Then, from (4.2) – (4.3),

$$u_1 = \frac{-rk_2 + \omega Lk_3}{2k_1}$$

$$u_2 = \frac{\omega Lk_2 + Rk_3 - e}{2k_1} \quad (4.4)$$

## 4.3. Integrability

Replacing (4.4) in (4.1) and taking into account that  $k(x) = \partial H_a(x) / \partial x$ , the following partial differential equation is obtained:

$$2I_0C\sqrt{2x_1}\left(\frac{\partial H_a}{\partial x_1}\right)^2 = -r\left(\frac{\partial H_a}{\partial x_2}\right)^2 - \left(r\frac{\partial H_a}{\partial x_3} - E\right)\frac{\partial H_a}{\partial x_3}$$

As we are interested in control inputs  $u_1, u_2$ , which only depend on the output voltage dc component, we take  $k_2 = k_2(x_1)$  and  $k_3 = k_3(x_1)$ . Then, by the Integrability condition,

$$\frac{\partial k_i}{\partial x_1} = \frac{\partial^2 H_a}{\partial x_1 \partial x_i} = \frac{\partial^2 H_a}{\partial x_i \partial x_1} = 0$$

for  $i = 2, 3$  and  $k_2 = a_2$  and  $k_3 = a_3$  are indeed constant. Thus, the PDE is actually an ODE on, whose solution is given by,

$$H_a(x) = -\frac{2}{3}\sqrt{\frac{2x}{I_0C}}x_1(a_2^2r + a_3^2r - a_3E) + a_2x_2 + a_3x_3 \quad (4.5)$$

#### 4.4 Equilibrium Assignment

From (4.3) and the definition of  $H_a$ , the following conditions on  $a_2, a_3$  and  $I_d$  so that  $x^*$ , from (4.2), is a singular point of  $H_d$  are derived

$$\frac{1}{C} + \frac{\sqrt{-2I_0C\sqrt{C^2V_d^2}(a_2^2r + a_3^2r - a_3E)}}{3I_0C\sqrt{C^2V_d^2}} = \frac{\sqrt{2}(a_2^2r + a_3^2r - a_3E)}{6\sqrt{-I_0C\sqrt{C^2V_d^2}((a_2^2r + a_3^2r - a_3E))}}$$

$$a_2 = 0 \text{ and } a_3 - I_d = 0.$$

This equations system has two solutions,

$$\left\{ a_2 = 0, I_d = \frac{E + \sqrt{E^2 - 8I_0V_d r}}{2r}, a_3 = I_d \right\}$$

$$\text{and } \left\{ a_2 = 0, I_d = \frac{E - \sqrt{E^2 - 8I_0V_d r}}{2r}, a_3 = I_d \right\}$$

Then, taking the latter solution,  $k_1$  and the control inputs derived in (4.3) are,

$$k_1 = - \frac{\sqrt{2} \sqrt{I_0^2 V_d C} \sqrt{2 x_1}}{2 I_0 C \sqrt{x_1}}$$

$$u_2 = -\frac{E + \sqrt{E^2 - 8I_0 v_d r C} \sqrt{V_0 V_d}}{4V_d}$$

## 5. SIMULATION RESULTS

Figure-2 shows the closed-loop structure of the IDA-PBA control approach. The actual rectifier is shown at the top of the figure with pulses as the input signal and the couple  $i_1(t)$  and  $v_0(t)$  as the output measured variables. The input voltage  $v_i(t)$  is sensed for being used as the input in the controller and the Inverse Discrete Fourier Transform (IDFT) blocks. The Recursive Discrete Fourier Transform (RDFT) allows the right Fourier Coefficients to be obtained at sampling intervals. The controller block computes the suitable averaged Fourier components for the control signal  $u(t)$  while the IDFT is performed in the IDFT block to obtain the discrete  $v(kT)$  control signal.

## 5.1 Response of uncontrolled and controlled bridge Rectifier

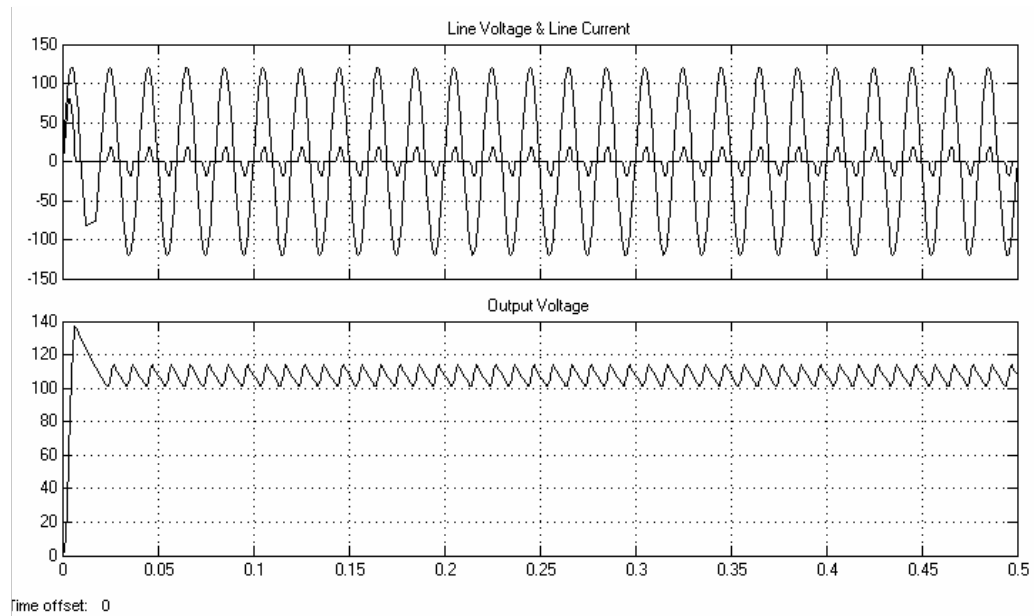


Figure 3. Response of the uncontrolled rectifier

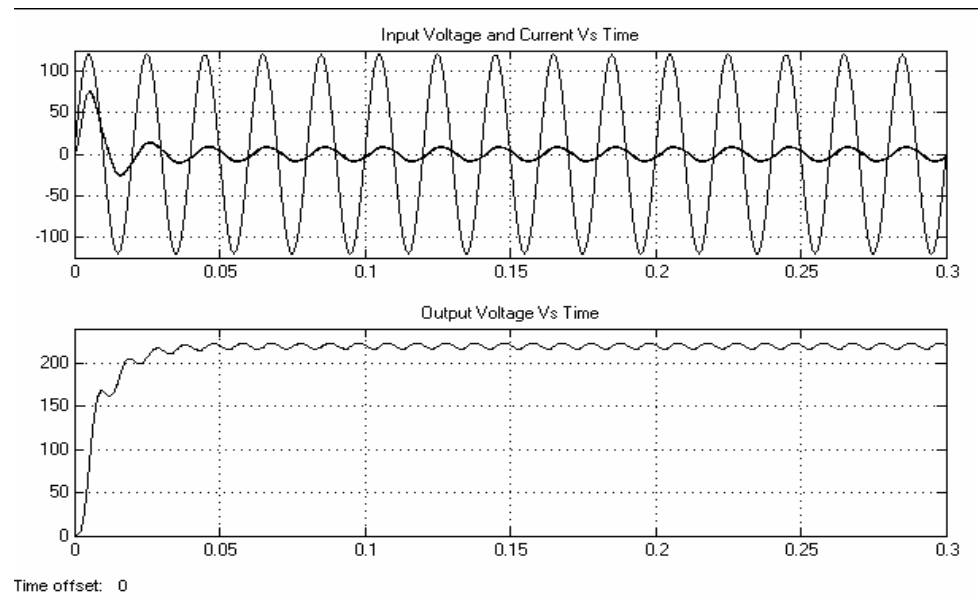


Figure 4. Open Loop Response of controlled bridge rectifier

As seen from the figure 3 and 4, the voltage output of the rectifier is less than the desired voltage and also the line current is not exhibiting the sinusoidal waveform. These drawbacks are overcome in the model proposed in this work.



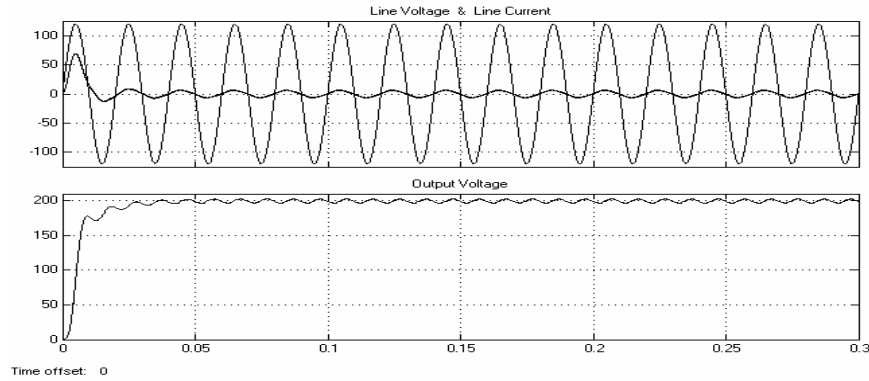


Figure 7 Unity power factor and voltage regulation responses

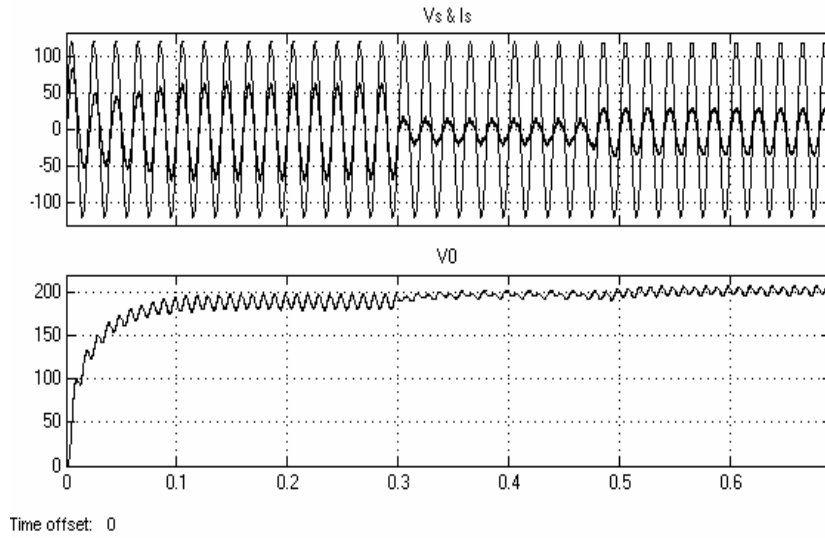


Figure 8 Responses for  $V_s$ ,  $I_s$  and  $V_o$  which exhibit robustness under load parameter variations ( $50 \Omega$  to  $500 \Omega$ )

The desired regulated DC output voltage and the power factor is  $V_o = 200V$  and near unity respectively. It is important to note that the power losses due to IGBT switches has been taken into account. The system performance could be improved by replacing these IGBT switches with low power ones.

### 5.3 Comparative discussions of the results

As seen from the figure 2 the line current of ordinary uncontrolled bridge rectifier is not sinusoidal, also there is no boost up of output voltage. However system itself is not robust and also the system power factor is also not unity (figure 3). But from figure 7, it's seen that using the proposed bridge rectifier model it's possible to get a sinusoidal line current and also boost up of output

voltage can also be done. From the figure 7, it's seen that by incorporating the controller it's possible to obtain robustness with respect to load variations and also it's possible to obtain a near unity power factor, figure 8. Initially, the DC bus voltage rests at the diode rectifier level with a resistive load of  $R = 60 \Omega$ . Then the control action is applied keeping the load resistance and the output voltage increases to the desired DC value. Afterwards two load changes from  $50 \Omega$  to  $500 \Omega$  were applied and the shape of the DC bus output voltage shows ensures the robustness of the controlled system with respect to load variations.

## 6. CONCLUSION

The performance analysis of single phase full bridge boost-type rectifier is analyzed for regulated output voltage and unity power factor at the AC mains. In the case considered here, a nonstandard tracking control problem for a full-bridge boost rectifier results in a regulation one because of GSSA expansion for phasor coefficients. An IDA-PB control has been designed measuring the load current and the load voltage, and presuming the input voltage is known. The closed-loop system is robust to load variations achieving unity power factor in the ac mains and load voltage Regulation.

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